

## Real Power Generation Scheduling of Thermal Power Plants for Economic Load Dispatch

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**Abstract-** In present days with increasing in load demand and with large interconnection of networks it is essential to run the generating stations optimally with in its constraints so as to meet the load demand. Without optimization the price for the cost of generation is increasing day to day. So it is very essential to reduce the running charges for generating electric energy. The main economic factor in power system planning, operation and control is with the cost of generating real power. The running cost will be the main consideration with respect to the fuel for thermal power plants, nuclear power plants and so on, whereas the running cost for hydro plants is negligible. So minimization of cost of real power generation will be criteria for thermal power plants.

A major objective for the thermal power generation is to minimize cost of real power generation by allocating optimal power generation to each unit (economic dispatch) subject to equality and inequality constraints. The optimum generation scheduling plays an extremely important role in optimal operation of utility power system. This importance is due to power savings. This paper proposed a lambda based approach for solving the Economic Dispatch (ED) problem. The ED is to minimize the cost of real power generation while satisfying the load demand and operational constraints. This paper solves sample test system of six generator system and 15 generator systems for various load demands including transmission losses.

**Index Terms-** Analytical method-lambda iterative method,  $P_G$ -real power generations,  $P_L$ -transmission loss, cost-cost of real power generations in Rs/Hr,  $P_D$ -load demand, ED-economic dispatch, EDC-economic dispatch computation

### I. INTRODUCTION

The size of electric power system is increasing rapidly to meet the energy requirements. A number of power plants are connected in parallel to supply the system load by interconnection of power stations. With the development of grid system it becomes necessary to operate the plant unit most economically [1]. The economic generation scheduling problem involves two separate steps namely the unit commitment and the online economic dispatch. The unit commitment is the selection of unit that will supply the anticipated load of the system

over a required period of time at minimum cost as well as provide a specified margin of the operating reserve. The function of the online economic dispatch is to distribute the load among the generating units actually paralleled with the system in such a manner as to minimize the total cost of the fuel [2]. To calculate electric power generation of various units with different load demands, the usual Kirchmayer's method is used. These are generally solved by iterating the value of until the sum of the generator outputs equals the system demand plus transmission losses [3]. The incremental transmission losses are calculated using transmission loss coefficient called B co-efficient approach [4]. Economic dispatch programs which are installed today in the most modern control centres uses the analytical methods to solve a well known exact co-ordination equations. The main difference between different techniques is the method used to solve the co-ordinations equations. The co-ordination equations are generally solved by interactively adjusting the load until the sum of the generator output matches the system load, pulse system loss [5]. A method named Quick method to optimize generation scheduling is discussed. It eliminates the iterative steps and offers a good savings in computer time and computer memory [6]. The analytical method to optimize generation schedule neglecting the transmission losses is discussed. Simplified approach to solution of co-ordination equation for generation scheduling is discussed [7]. The transmission loss penalty factor have been implemented using one of the several loss formulas which are calculated off-line or on-line at periodic interval and on request [8]. New graphical method for optimum power generation with neglecting the mutual elements of B-coefficient matrix is discussed [9].

### II. OBJECTIVE FUNCTION

The cost of power generation is not the same for every unit. So, to have the minimum cost of generation for a particular load demand, we have to distribute the load among the units which minimize the overall generation cost with the constraint that no unit is overloaded. Economic dispatch, by definition is an on-line function, carried out after every 15-30 minutes or on request in Power Control Centres. It is defined as the process of calculating the power generation of the generating units in the system in such a way that the total system demand is supplied

most economically. It is the standard industrial practice that the fuel cost of generator is represented

by polynomial for economic dispatch computation (EDC) [2]. The objective function of this paper is

$$C_i = a_i P_{Gi}^2 + b_i P_{Gi} + d_i \dots (1)$$

Where  $a_i$  is a measure of losses in the system,  $b_i$  is the fuel cost and  $d_i$  is the salary and wages, interest and depreciation.

The optimal dispatches for the thermal power plants should be such that the total electric power generation equal to the load demand plus line losses, which can be written as:

$$\sum_{i=1}^n P_{Gi} - PD - PL = 0 \dots (2) \text{ Where } n = \text{total number}$$

of generating plants,  $P_{Gi}$  = generation of  $i^{\text{th}}$  plant,  $PL$  = total system transmission loss,  $PD$  = system load demand. The transmission losses which occur in the line when power is transferred from the generating station to the load centres increases with increase in distance between the two [6, 7, 8]. The transmission losses may vary from 5 to 15 % of the total load. If the power factor of load at each bus is assumed to remain constant the system loss  $PL$  can be shown to be a function of active power generation at each plants i.e.

$$P_L = P_L(P_{G1}, P_{G2}, \dots, P_{GK}) \dots (3)$$

One of the most important, simple but approximate method of expressing transmission loss as a function of generator powers is through B-Coefficients and is given by Kron's loss formula [1] as:

$$P_L = \sum_{i=1}^n \sum_{j=1}^n P_{Gi} B_{ij} P_{Gj} \dots (4)$$

Where,  $P_{Gi}$ , &  $P_{Gj}$  are real power generation at  $i^{\text{th}}$  and  $j^{\text{th}}$  power unit.  $B_{ij}$  is loss coefficients.

The inequality constraints is given by

$$P_{GiMin} \geq P_{Gi} \geq P_{GiMax} \dots (5)$$

Maximum active power generation  $P_{GiMax}$

Minimum active power generation  $P_{GiMin}$

### III. METHODOLOGY

The objective of optimum generation scheduling for thermal power plants is to allocate the generation to each and every units in a plant for a given load such that the cost of real power generation is minimum subjected to equal and inequality constraints. Here, optimum generation scheduling is achieved by following technique. This is an iterative and an accurate method to determine output of generator. An algorithm for obtaining real power generation and fuel cost are iteratively solved on the following steps for a particular load demand [8].

The Algorithm is as follows:

1. Start
2. Initially chose  $\lambda = \lambda_0$ , this value should be greater than the largest intercept of the incremental cost of the various units. Calculate  $P_{G1}, P_{G2}, P_{Gi}$  based on equal incremental cost.
3. Assume  $P_{Gi} = 0.0$ ;  $i=1, 2 \dots N$
4. Read the constants  $a_i, b_i$ , loss coefficient matrices  $B_{ij}$ , and  $B_{0i}$ , constant  $B_{00}$ , power demands  $P_D$ , maximum  $P_{GiMax}$ , minimum  $P_{GiMin}$  generators real power limits

5. Calculate the generation at all buses using

$$P_{Gi} = (1 - B_{0i} - b_i / \lambda - \sum_{j=1}^k 2B_{ij} P_{Gj}) / (2a_i / \lambda + 2B_{ij}) \text{ where } i=1, 2, \dots, k \dots (6)$$

keeping in mind that the values of powers to be substituted on the RHS of Eq.(6) during zero iteration correspond to the values calculated in step 2. For subsequent iterations the values of powers to be substituted corresponds to the powers in the previous iteration. However if any generator violates the limit of generation that generator is fixed at the limit violated.

6. Check if the difference in power at all generator buses between two consecutive iterations is less than the specified value, otherwise go back to step 2.

7. Calculate power loss using Eq. (7)

$$P_L = \sum_{i=1}^n \sum_{j=1}^n P_{Gi} B_{ij} P_{Gj} \dots (7)$$

8. Check if power balance equation is satisfied,

$$\sum_{i=1}^n P_{Gi} - PD - PL < \epsilon \dots (8)$$

if yes, stop. Otherwise, go to step-9.

9. Increase  $\lambda$  by  $\Delta\lambda$ ; if

$$\sum_{i=1}^n P_{Gi} - PD - PL < 0 \dots (9)$$

decrease  $\lambda$  by  $\Delta\lambda$ ; if

$$\sum_{i=1}^n P_{Gi} - PD - PL > 0 \dots (10)$$

10. Repeat from step 5

11. Update  $\lambda$  as  $\lambda^{(k+1)} = \lambda^{(k)} - \Delta\lambda^{(k)}$  where  $\lambda$  is the step size

12. Stop.

### IV. TEST SYSTEMS

Here we consider two test systems. In the first case 6 generators are considered with their cost curve equations and its loss coefficients (B coefficients). In the second case 15 generators are considered with their cost curve expression along with its loss coefficients. The optimum generation scheduling for different load conditions is explained here. The optimal generation scheduling of 6 thermal generating units and 15 thermal generating units for different loads are determined.

#### Test case I:

The cost of real power generation and transmission loss for six generating units for different load conditions is determined. The result for different load conditions is given in table 4.1. From the tabular column it is cleared that all generators are operating within its constraint limits.

$P_{DT}$	955	942	935	930	935	963
	379.1	375.93	374.21	372.98	374.21	381.09
	282	57	71	97	71	32
$P_{G1}$	128.0	125.56	124.24	123.31	124.24	129.50
$P_{G2}$	017	15	81	02	81	39

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<b>P<sub>G3</sub></b>	210.9 572	208.49 04	207.16 23	206.21 39	207.16 23	212.47 55
<b>P<sub>G4</sub></b>	83.42 09	80.842	79.453 9	78.462 6	79.453 9	85.008 5
<b>P<sub>G5</sub></b>	109.8 925	107.40 25	106.06 12	105.10 3	106.06 12	111.42 43
<b>P<sub>G6</sub></b>	50	50	50	50	50	50
<b>cost</b>	68453 3.4	674787	669555	665823 .6	669555	690549 .6
<b>P<sub>L</sub></b>	6.400 5	6.2321	6.1426	6.0792	6.1426	6.5055

Table 4.1 Generations, cost & power loss for various loads

The result for different load conditions is given in table 4.2. From the tabular column it is cleared that all generators are operating within its constraint limits. It means that all generators are operating economically.

<b>P<sub>DT</sub></b>	<b>989</b>	<b>1023</b>	<b>1126</b>	<b>1150</b>	<b>1201</b>	<b>1235</b>
<b>P<sub>G1</sub></b>	387.4 821	395.66 71	417.06 15	422.05 74	432.68 75	439.78 44
<b>P<sub>G2</sub></b>	134.3 892	139.20 25	155.07 41	158.78 05	166.66 7	171.93 24
<b>P<sub>G3</sub></b>	217.4 117	222.65 9	238.80 68	242.57 48	250.58 86	255.93 62
<b>P<sub>G4</sub></b>	90.17 13	95.818 8	112.78 56	116.74 84	125.18 11	130.81 18
<b>P<sub>G5</sub></b>	116.3 998	121.40 96	137.52 27	141.27 18	149.23 22	154.53 41
<b>P<sub>G6</sub></b>	50	55.459 1	73.142 3	77.257 2	85.994 4	91.814
<b>cost</b>	71019 9	736102 .8	815854 .2	834712 .8	875134 .8	902344 .8
<b>P<sub>L</sub></b>	6.854 2	7.2159	8.3929	8.6901	9.3507	9.8129

Table 4.2 Generations, cost & power loss for various loads

The result for different load conditions is given in table 4.3. From the tabular column it is cleared that all generators are operating within its constraint limits.

<b>P<sub>DT</sub></b>	<b>1190</b>	<b>1251</b>	<b>1263</b>	<b>1250</b>	<b>1221</b>	<b>1202</b>
<b>P<sub>G1</sub></b>	430.3 931	443.12 7	445.63 52	442.91 81	436.86 12	432.89 61
<b>P<sub>G2</sub></b>	164.9 648	174.41 24	176.27 32	174.25 73	169.76 35	166.82 17
<b>P<sub>G3</sub></b>	248.8 593	258.45 41	260.34 32	258.29 67	253.73 37	250.74 58

<b>P<sub>G4</sub></b>	123.3 609	133.46 4	135.45 41	133.29 81	128.49 24	125.34 66
<b>P<sub>G5</sub></b>	147.5 16	157.02 77	158.89 74	156.87 19	152.35 15	149.38 82
<b>P<sub>G6</sub></b>	84.11 06	94.551 2	96.603 5	94.380 1	89.418 2	86.165 6
<b>cost</b>	86637 6	915222 .6	924911 .4	914416 .2	891115 .2	875931 .6
<b>P<sub>L</sub></b>	9.204 9	10.036 4	10.206 6	10.022 3	9.6205	9.364

Table 4.3 Generations, cost & power loss for various loads

The result for different load conditions is given in table 4.4. From the tabular column it is cleared that all generators are operating within its constraint limits.

<b>P<sub>DT</sub></b>	<b>1159</b>	<b>1092</b>	<b>1023</b>	<b>984</b>	<b>975</b>	<b>960</b>
<b>P<sub>G1</sub></b>	423.9 32	409.99 09	395.66 71	386.25 32	384.04 15	380.35 63
<b>P<sub>G2</sub></b>	160.1 712	149.82 86	139.20 24	133.44 94	131.75 81	128.94 05
<b>P<sub>G3</sub></b>	243.9 883	233.47 22	222.65 89	216.46 22	214.75 35	211.90 61
<b>P<sub>G4</sub></b>	118.2 354	107.17 77	95.818 8	89.178 1	87.390 8	84.413 1
<b>P<sub>G5</sub></b>	142.6 773	132.20 78	121.40 95	115.44 33	113.72 13	110.85
<b>P<sub>G6</sub></b>	78.79 97	67.309 3	55.459 1	50	50	50
<b>cost</b>	84181 2	789316 .2	736102 .8	706408 .8	699600	688291 .8
<b>P<sub>L</sub></b>	8.803 8	7.9866	7.2159	6.7863	6.6651	6.466

Table 4.4 Generations, cost & power loss for various loads

Fig 1 shows the relation for time in hrs and cost of real power generations of six units for 24 hrs to meet the load demand.

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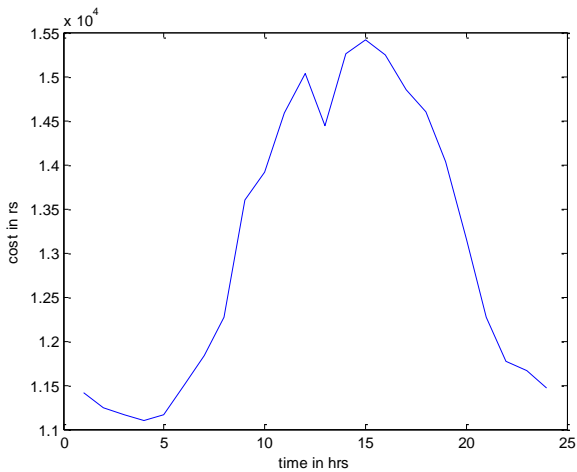


Fig 1. Time vs Cost real power generations of all units

The fig 2 clearly shows that during peak load hrs the cost for real power generation is high, i.e., all generator generate maximum power at peak loads.

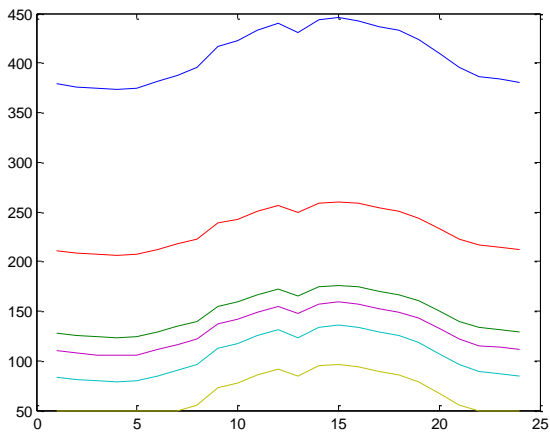


Fig 2. Time vs Real power generations of all units

The graphs explains during peak load hrs cost of generation also increases.

### Test case II:

The result for different load conditions is given in table 4.5. From the tabular column it is cleared that all generators are operating within its constraint limits.

$P_{DT}$	2236	2240	2226	2236	2298	2316
$P_{G1}$	455	455	455	455	455	455
$P_{G2}$	455	455	455	455	455	455
$P_{G3}$	130	130	130	130	130	130
$P_{G4}$	130	130	130	130	130	130
$P_{G5}$	150	150	150	150	150	150
$P_{G6}$	460	460	460	460	460	460
$P_{G7}$	465	465	465	465	465	465
$P_{G8}$	60	60	60	60	60	60

$P_{G9}$	25	25	25	25	25	25
$P_{G10}$	160	160	160	160	160	160
$P_{G11}$	80	80	80	80	80	80
$P_{G12}$	20	20	20	20	20	20
$P_{G13}$	25	25	25	25	25	25
$P_{G14}$	15	15	15	15	15	15
$P_{G15}$	15	15	15	15	15	15
cost	19490 81	194908 1	194908 1	194908 1	194908 1	194908 1
$P_L$	22.65 04	22.650 4	22.650 4	22.650 4	22.650 4	22.650 4

Table 4.5 Generations and cost of generations for various loads

The result for different load conditions is given in table 4.6. From the tabular column it is cleared that all generators are operating within its constraint limits.

$P_{DT}$	2331	2443	2630	2728	2783	2785
$P_{G1}$	455	455	455	455	455	455
$P_{G2}$	455	455	455	455	455	455
$P_{G3}$	130	130	130	130	130	130
$P_{G4}$	130	130	130	130	130	130
$P_{G5}$	150	150	150	150	150	150
$P_{G6}$	460	460	460	460	460	460
$P_{G7}$	465	465	465	465	465	465
$P_{G8}$	60	60	60	60	60	60
$P_{G9}$	25	25	25	25	25	25
$P_{G10}$	160	160	160	160	160	160
$P_{G11}$	80	80	80	80	80	80
$P_{G12}$	20	20	27.575 5	80	80	80
$P_{G13}$	25	25	25	25	25	25
$P_{G14}$	15	15	15	15	15	15
$P_{G15}$	15	15	15	15	15	15
cost	19490 81	194908 1	195370 1	198670 6	198670 6	198670 6
$P_L$	22.65 04	22.650 4	22.575 5	22.227 4	22.227 4	22.227 4

Table 4.6 Generations and cost of generations for various loads

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The result for different load conditions is given in table 4.7. From the tabular column it is cleared that all generators are operating within its constraint limits.

P <sub>DT</sub>	2780	2830	2970	2950	2902	2803
P <sub>G1</sub>	455	455	455	455	455	455
P <sub>G2</sub>	455	455	455	455	455	455
P <sub>G3</sub>	130	130	130	130	130	130
P <sub>G4</sub>	130	130	130	130	130	130
P <sub>G5</sub>	150	150	450.91 36	450.91 36	150	150
P <sub>G6</sub>	460	460	460	460	460	460
P <sub>G7</sub>	465	465	465	465	465	465
P <sub>G8</sub>	60	60	60	60	60	60
P <sub>G9</sub>	25	25	25	25	25	25
P <sub>G10</sub>	160	160	160	160	160	160
P <sub>G11</sub>	80	80	80	80	80	80
P <sub>G12</sub>	80	80	80	80	80	80
P <sub>G13</sub>	25	25	25	25	25	25
P <sub>G14</sub>	15	15	15	15	15	15
P <sub>G15</sub>	15	15	15	15	15	15
cost	19867 06	198670 6	217670 0	217670 0	198670 6	198670 6
P <sub>L</sub>	22.22 74	22.227 4	35.913 6	35.913 6	22.227 4	22.227 4

Table 4.7 Generations and cost of generations for various loads

The result for different load conditions is given in table 4.8. From the tabular column it is cleared that all generators are operating within its constraint limits.

P <sub>DT</sub>	2651	2584	2432	2312	2261	2254
P <sub>G1</sub>	455	455	455	455	455	455
P <sub>G2</sub>	455	455	455	455	455	455
P <sub>G3</sub>	130	130	130	130	130	130
P <sub>G4</sub>	130	130	130	130	130	130
P <sub>G5</sub>	150	150	150	150	150	150
P <sub>G6</sub>	460	460	460	460	460	460
P <sub>G7</sub>	465	465	465	465	465	465
P <sub>G8</sub>	60	60	60	60	60	60

P <sub>G9</sub>	25	25	25	25	25	25
P <sub>G10</sub>	160	160	160	160	160	160
P <sub>G11</sub>	80	80	80	80	80	80
P <sub>G12</sub>	48.40 17	20	20	20	20	20
P <sub>G13</sub>	25	25	25	25	25	25
P <sub>G14</sub>	15	15	15	15	15	15
P <sub>G15</sub>	15	15	15	15	15	15
cost	19665 95	194908 1	194908 1	194908 1	194908 1	194908 1
P <sub>L</sub>	22.40 17	22.650 4	22.650 4	22.650 4	22.650 4	22.650 4

Table 4.8 Generations and cost of generations for various loads

Fig 3 shows the relation for time in hrs and cost of power generations of 15 units for 24 hrs to meet the load demand.

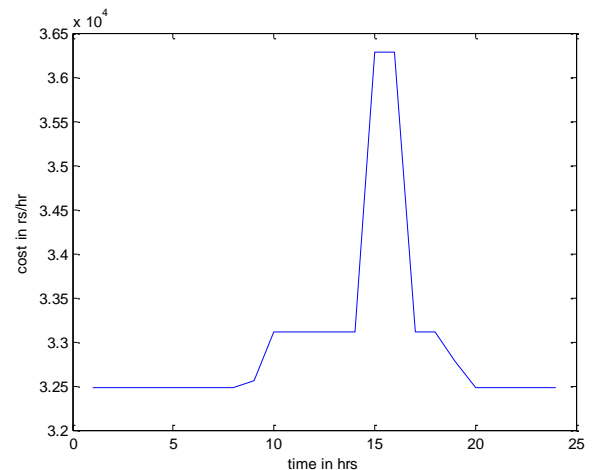


Fig 3. Time vs Cost of real power generations of all units

It shows that during peak hours when the load demand is high the cost of generating real power increases.

### V CONCLUSION

This paper deals with optimal generation scheduling in thermal power plants with minimum cost of real power generation. The equality and inequality constraints are considered while optimizing generation scheduling. The constant B- Coefficients are used to find the transmission loss. In both case studies it is clear that all generators run within its constraint limits for optimum generation allocation or economic load dispatch. If the generators do not run in its constraint limits whether below its minimum generation capacity or above its maximum generation capacity economic load dispatch is not possible. Therefore economic load dispatch is possible only if all generating units run within its constraints limits.

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